

Evidence for Pairing above the Transition Temperature of Cuprate Superconductors from the Electronic Dispersion in the Pseudogap Phase

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In the underdoped high temperature superconductors, instead of a complete Fermi surface above T_c , only disconnected Fermi arcs appear, separated by regions that still exhibit an energy gap. We show that in this pseudogap phase, the energy-momentum relation of electronic excitations near E_F behaves like the dispersion of a normal metal on the Fermi arcs, but like that of a superconductor in the gapped regions. We argue that this dichotomy in the dispersion is difficult to reconcile with a competing order parameter, but is consistent with pairing without condensation.

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There is no consensus regarding the origin of the pseudogap [1–3] in underdoped cuprates. The arguments can be distilled into two general ideas [4]: the pseudogap arises either from pairing of electrons [5,6] in a state precursor to superconductivity or from an alternate order parameter [7–9]. Lacking a direct measurement of the momentum-dependent pairing correlations, we ask whether some features unique to Cooper pairing are present in the electronic excitation spectrum above T_c . In particular, the dispersion of states of energy ϵ and momentum \mathbf{k} in the normal state, shown schematically in Fig. 1(a) as a parabola, is usually linear for a small energy interval near the Fermi energy. The locus of Fermi crossings, the Fermi surface, is shown in Fig. 1(b). In the superconducting state, the linear dispersion transforms into the Bogoliubov dispersion $E_k = \pm\sqrt{\epsilon_k^2 + \Delta_k^2}$, shown as solid curves in Fig. 1(a), where Δ_k is the gap function. The minimum in the excitation energy along a momentum cut normal to the Fermi surface is at $|\Delta_k|$, which occurs at \mathbf{k}_F , the Fermi momentum of the normal state. This is a consequence of the fact that the pairs condense with a zero center of mass momentum.

The Bogoliubov dispersion below T_c can be readily observed in experimental angle resolved photoemission (ARPES) spectra [10], as shown in Fig. 1(c) [11]. The excitation energy, E_k , approaches E_F , but instead of crossing it, it reaches a minimum value at \mathbf{k}_F , before receding away from E_F , where it remains only visible for a small range of \mathbf{k} beyond \mathbf{k}_F . These new states result from the mixing of electrons with holes, as shown in Fig. 1(a). Even the Bogoliubov dispersion branch above E_F has been seen in ARPES by thermal population [12].

An important consequence of particle-hole mixing with zero center-of-mass momentum is that the minimum gap location is identical to the normal state Fermi momentum. Figure 2(a) shows the dispersion in the superconducting

state at $T = 40$ K for a $T_c = 90$ K sample over the entire Brillouin zone. This dispersion was obtained as follows. The ARPES spectrum is proportional to the product of the single-particle spectral function and the Fermi function, convolved with the instrumental resolution. We therefore

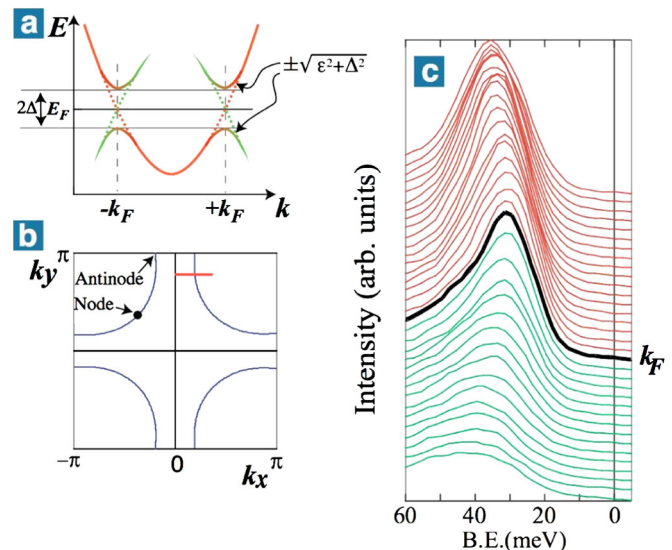


FIG. 1 (color online). (a) Schematic of the normal state dispersion (dashed curve) which acquires a gap with a characteristic Bogoliubov dispersion in the superconducting state (solid curves). (b) Fermi surface in the Brillouin zone, identifying where the d -wave gap is zero (node) and where it is maximal (antinode). (c) Energy distribution curves (EDCs) in the superconducting state ($T = 17$ K) of a thin film $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ ($\text{Bi}2212$) sample with $T_c = 80$ K along the momentum cut identified in (b). Each curve corresponds to an increase in momentum of 0.003 \AA^{-1} . The EDC at \mathbf{k}_F is indicated by the thick curve. The data were taken with a Scientia R4000 analyzer with 22 eV photons.

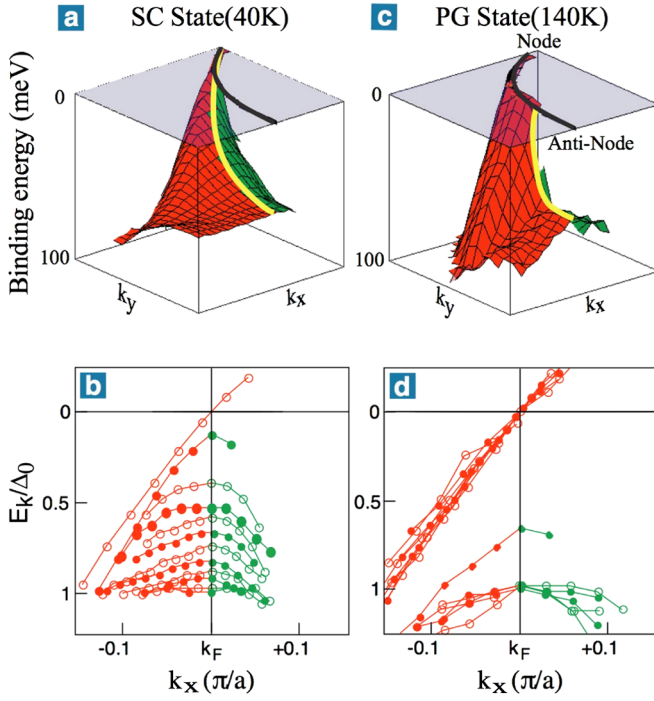


FIG. 2 (color online). (a) Binding energy of the spectral peak from Fermi function divided ARPES data for a Bi2212 single crystal with $T_c = 90$ K as a function of (k_x, k_y) in the superconducting state at $T = 40$ K. The dispersion minima are plotted as a curve on the dispersion surface, with its projection onto the top face also shown, which is equivalent to the normal state Fermi surface. (b) Cuts for various k_y from (a), showing the peak dispersion versus k_x . (c) Data same as in (a), but in the pseudogap phase ($T = 140$ K). (d) Cuts for various k_y from (c), showing the peak dispersion vs k_x . Note that the dispersion either crosses E_F (along the Fermi arc) or exhibits Bogoliubov-like behavior similar to the superconducting state. The data were taken with a Scienta SES 200 electron analyzer with 22 eV photons.

take the raw spectra and divide this by a resolution broadened Fermi function obtained by fitting a reference gold spectrum in electrical contact with the sample that is used to determine the chemical potential. The peak positions of these divided spectra define our dispersion, which we show below E_F in Fig. 2(a). The forward surface in this plot represents the particlelike region of the dispersion, while the holelike region is behind. The top face of the cube is the chemical potential (E_F). The spectral peak crosses E_F only at one point (the node), while the spectra at other momenta are gapped. The curve on the dispersion surface shows the dispersion minima, which to a good approximation follow the simple d -wave gap function $|\Delta_{\mathbf{k}}| = \Delta_0 |\cos k_x a - \cos k_y a|/2$ where Δ_0 is the maximum d -wave gap. The curve on the top face shows the location where these minima occur in the Brillouin zone, which coincides with the normal state Fermi surface, \mathbf{k}_F . In Fig. 2(b), we show cuts from Fig. 2(a) at regular k_y intervals, where the back bending is clearly seen in all cuts for k_x beyond k_F , except at the node.

We now turn to the pseudogap phase, where in Fig. 2(c), we show the dispersion taken at $T = 140$ K. In contrast to the superconducting state, the dispersion now crosses E_F for an extended length, forming a Fermi arc [13,14]. This arc extends from the node to approximately half way to the antinode. The rest of the spectra are gapped. Moreover, we find the remarkable fact that where it is gapped, the dispersion shows back bending characteristic of the superconducting state. In Fig. 2(d), the momentum cuts of the dispersion for various k_y in the pseudogap phase are shown. Note that for each cut where a gap exists, the bending back behavior is present.

This is a remarkable situation—the dispersion in part of the Brillouin zone (on the arc) behaves as if the sample were a normal metal, while in the remainder of the zone, where the pseudogap is well established, the dispersion behaves as if the sample were superconducting even though we are above T_c . To further emphasize this dichotomy, we show in Fig. 3(a) the Fermi function divided spectra for a momentum cut through the Fermi arc, as indicated in the inset. The spectral peak disperses through E_F in the normal state, showing no indication of a gap. The relatively high-sample temperature of 140 K allows us to follow the dispersion for some distance above E_F . The spectral peak is never observed to bend back. In contrast, in a cut through the gapped portion of the normal state Fermi surface shown in Fig. 3(b), the dispersion (arrows) clearly exhibits the characteristic bending back of the superconducting state. The spectral peak approaches E_F , reaches a minimum, and then recedes.

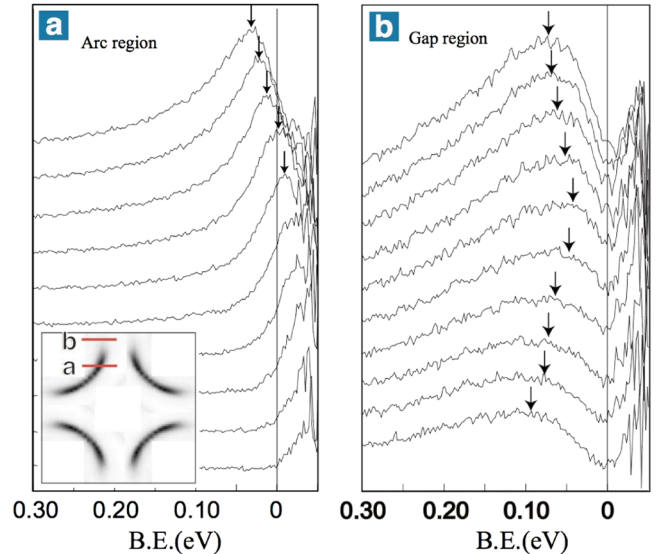


FIG. 3 (color online). Dispersion of the Fermi function divided EDCs for a Bi2212 single crystal with $T_c = 90$ K in the pseudogap phase ($T = 140$ K) along (a) cut “a” shown in the inset which crosses the Fermi arc (the gray shading in the inset indicates the intensity at E_F), and (b) cut “b” shown in the inset of (a) that crosses k_F in the gapped region. Each curve corresponds to an increase in momentum of 0.01 \AA^{-1} .

It is important to compare the dispersions in the superconducting and pseudogap phases. In Figs. 4(a) and 4(b), we show raw photoemission spectra (not divided by the Fermi function) from a Bi2212 film with $T_c = 80$ K, taken at the momentum cut shown in Fig. 4(c). The superconducting state spectra are shown to the left of zero energy, while the pseudogap phase spectra are reflected to the right of zero energy. Each pair of curves in the superconducting and pseudogap phases were obtained at the same \mathbf{k} point. A key difference between panels (a) and (b) is in the spectral linewidths: there is a narrow quasiparticle peak below T_c , while the pseudogap spectra are broad, indicating a short electronic lifetime [14]. Nevertheless, the dispersions in both panels exhibit the same characteristic bending back behavior. More importantly, the dispersion minima in both the pseudogap and superconducting phases occur at the same \mathbf{k} , which happen to be the \mathbf{k}_F of the normal state [10]. We find that for all samples we have investigated, the minimum gap occurs exactly at the same \mathbf{k} above and below T_c for all cuts, irrespective of their position along the Fermi surface.

We now discuss the implications of our results. It has been suggested that the pseudogap originates from some ordering phenomenon—unrelated to superconductivity—characterized by a wave vector \mathbf{Q} . Let us look at the case

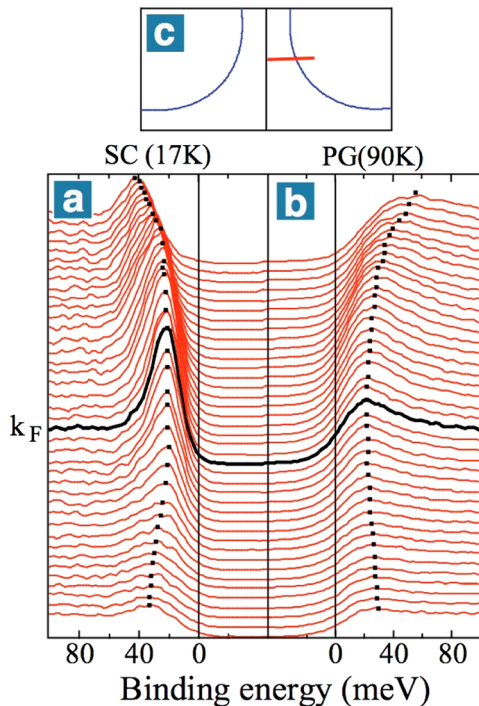


FIG. 4 (color online). EDCs in (a) the superconducting state ($T = 17$ K) and (b) the pseudogap phase ($T = 90$ K) of a Bi2212 film with $T_c = 80$ K for the cut in the zone shown in (c). The thick curves in (a) and (b) represent the minimum gap location, and can be seen to occur at the same value of k , corresponding to the normal state k_F . Note that for this cut, the Fermi surface has already started to curve away from the flat regions near the antinode.

[15] of a \mathbf{Q} that spans flat parts of the Fermi surface near the antinode, where the pseudogap is maximal, as shown in Fig. 5(a). This, and other suggestions regarding the origin of the pseudogap, requires us to consider whether evidence for such a \mathbf{Q} vector exists in the data. Now, as soon as the spanning vector between the Fermi surfaces becomes significantly longer than \mathbf{Q} , the states near E_F will no longer be gapped. However, as shown in Fig. 4(b), the dispersion for a momentum cut where the Fermi surfaces are separated by a vector longer than \mathbf{Q} (i.e., for a k point not on the flat part of the Fermi surface) still shows back bending after reaching a minimum at the same \mathbf{k} as the normal state \mathbf{k}_F .

Moreover, the alteration of the dispersion resulting from an ordering vector \mathbf{Q} is not limited to the region near \mathbf{k}_F and E_F , as it is in the case of superconductivity. Because \mathbf{Q} mixes states at \mathbf{k} with those at $\mathbf{k} \pm \mathbf{Q}$, additional Fermi sheets are present which are images of the Fermi surface displaced by $\pm \mathbf{Q}$. We do not see these “umklapps,” even close to the Fermi surface where the mixing is strong enough that their intensity should be observable by ARPES, as they are in metals which do exhibit a density wave instability [16]. Moreover, such ordering has the unavoidable consequence of shifting the gap *away* from E_F when the Fermi surfaces are spanned by a vector longer than \mathbf{Q} , as shown in Fig. 5(b). Since the Fermi surface is holelike, this gap appears *below* E_F and thus should be observed by ARPES if it existed. We find no evidence for such a gap.

We emphasize that these arguments cast doubt on any $\mathbf{Q} \neq 0$ order as the origin of the pseudogap. We are thus left with the likelihood that the observed Bogoliubov-like

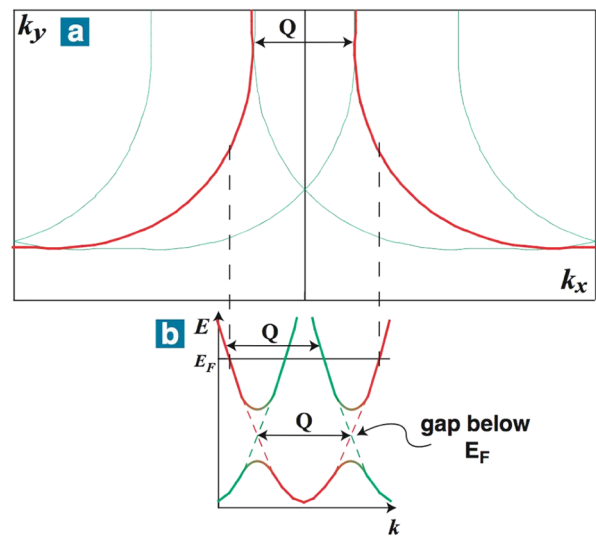


FIG. 5 (color online). (a) The Fermi surface curves umklapped by $\pm \mathbf{Q}$, with \mathbf{Q} chosen so as to span the Fermi surface in its flat parts near the antinode. (b) Schematic of the dispersion along a cut where the separation between the two Fermi surfaces becomes larger than $|\mathbf{Q}|$, that is between where the dashed vertical lines intersect the Fermi surface in (a). Note that a gap forms below the Fermi energy, and thus would be observable by ARPES if it existed.

dispersion above T_c is the analog of particle-hole mixing below T_c arising due to short-range superconducting order. This would naturally explain why the minimum gap *always* occurs at \mathbf{k}_F in momentum space and why the corresponding spectral function has a minimum at E_F .

In conventional BCS superconductors, the breaking up of the Cooper pairs is responsible for the phase transition at T_c since the energy gap is much smaller than the phase stiffness, which is controlled by the superfluid density. In contrast, as suggested early on by Uemura *et al.* [17], it is the small superfluid density in the underdoped cuprates which determines the loss of phase coherence at T_c , an idea which is further substantiated by recent measurements in highly underdoped materials [18,19] and the non-mean-field behavior of the specific heat near T_c [20]. In these materials, the pairing gap is much larger than the superfluid density, and thus pairing survives above T_c . Recent examples of possible observations of pairing without phase coherence are in systems as diverse as granular superconductors [21] and cold atomic Fermi gases [22].

To what extent are other experiments on underdoped cuprates consistent with the idea of pairing of electrons above T_c in the pseudogap phase? Early NMR experiments [23,24] showed a freezing out of the spin susceptibility and the relaxation rate $1/T_1T$ with decreasing T . This directly implies the formation of singlet pairs with an onset temperature well above T_c , and consistent with T^* at which the pseudogap becomes observable in ARPES [2,3] and in the STM tunneling density of states [25]. More recently, there have been two important experiments on the existence of fluctuating superconducting regions in the pseudogap phase: the direct observation of diamagnetism above T_c [26] and an anomalously large Nernst signal [27] attributed to vortices above T_c . The Nernst onset temperature, though larger than T_c , is definitely lower than T^* and has a different doping dependence; it goes to zero close to the doping where superconductivity disappears, while T^* and the ARPES pseudogap continue to increase in magnitude with underdoping. We believe that there is no contradiction here; in addition to pairing, the Nernst effect also needs local phase coherence over large enough spatial regions for the vortices to exist.

We note that at the present time there is no complete theory of the remarkable dichotomy of the dispersion that we observe in different parts of momentum space, including the temperature dependence of the arcs [14] and the closing of the gap along the arcs versus its filling in elsewhere [28,29]. On quite general grounds, we expect that the ARPES spectral function only involves the average $\langle |\Delta_{\mathbf{k}}|^2 \rangle$, which is finite even when the phase of the order parameter is fluctuating, thus leading to a characteristic back bending of the dispersion above T_c . The \mathbf{k} -space anisotropy of the pseudogap and dispersion are nevertheless closely linked to the d -wave anisotropy of the gap—it is expected that the gap around the node will be more

susceptible to fluctuations than the gap around the antinode because of its smaller magnitude.

In summary, we found a Bogoliubov-like dispersion in the pseudogap phase of the high temperature cuprate superconductors, despite the fact that there are no sharply defined quasiparticles above T_c . This anomalous dispersion leads us to conclude that pairing, without long range phase order, underlies the pseudogap below T^* . On the other hand, superconductivity below T_c arises from the locking of the phase of all the pairs forming a condensate with long-range order.

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