Dynamic Modeling And Control Of A Residential Solar Thermal Electrical Generator With Cogeneration

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Abstract

This thesis focuses on studying, through experiments and simulations, the feasibility of a small scale, residential thermal solar system for renewable energy capture. The work builds upon efforts conducted over the last 18 months for sourcing components for this thermal solar system and on the identification through thermodynamic simulations of appropriate working fluids for the low temperature organic Rankine cycle suited for thermal solar power generation. The work conducted in this thesis focuses on two complementary aspects. First, the experimentation with a first generation prototype consisting of a primary loop to capture the solar energy with a manifold of evacuated tubes, of thermal energy buffer and a secondary loop mimicking the energy input into an actual Rankine cycle. The data collected from this experimental setup is used to calibrate and validate a modeling effort. The second aspect of this work is the development of a dynamic model in Simulink of the thermal solar system, which can be used as a basis for system control and optimization. The dynamic component of this simulator significantly expands the earlier work done at steady state only, as the solar energy (input) and electricity demand (output) vary significantly with the time of the day, day of the year, weather conditions, etc. and are not synchronized. This temporal mismatch between the solar radiation and the electrical demand necessitates an energy buffer and energy management control strategy to maximize the utility of this residential solar plant. The further challenge stems from the need for a phase change (boiling/condensing) of the working fluid (R-600a – isobutane in this case) with the temperatures reachable within the solar collection system, and hence enabling an organic Rankine cycle to generate power.
This study, while hampered by hardware shortcomings and an unusually cold and rainy testing period, achieved most of the objective of this study: the construction, instrumentation, data acquisition of a fully functioning primary loop, thermal storage unit and secondary loop. Furthermore, a dynamic model (in Simulink) was developed and partially calibrated with the sparse experimental data available and is fully functional, enabling the control system development, optimization and energy management effort to follow.
Acknowledgements

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Chapter 1: Introduction

1.1 Motivation

Energy is the lifeblood of our modern society. Using energy we have built tall skyscrapers, flown to the moon, dove to the bottom of the oceans, and split atoms to their smallest constituents. Unfortunately, it is not infinite and it is not free. Life as we know it today could literally not exist without the untold volumes of fossil fuels, biomass, and nuclear material. Those sources give off harmful emissions while being used (except uranium), and leave waste material that can be incredibly harmful to human health and the environment. The recent incident in the Gulf of Mexico and indications that we may have already reached peak oil output capacity paint a grim picture for the future of liquid hydrocarbons. In addition, the continuous improvement in battery and fuel cell technology could accelerate the development of electric vehicles, increasing demand for electricity. The more recent tragedy in Japan, leading to the possible partial meltdown of at least three nuclear reactors may be a death blow to the proposed nuclear renaissance. Figure 1 shows domestic energy use (all sectors) by fuel type. Needless to say, it does not paint a bright picture when showing America’s dependence on these consequence heavy fuels. Additionally, Figure 2 shows that peak oil could be happening now, though other reports have it occurring at later dates, few dispute that it will not happen in the next couple of decades. In the US, coal generates 45% of electricity as shown in Figure 3. Coal even in its cleanest forms and burned efficiently, is an inherently dirty source of energy. In addition to CO2, it outputs soot, ash, NOx, sulfates and is actually more radioactive than a nuclear power plant to the surrounding community. Those factors alone are bad, but when the devastation wrought by mountain top mining is realized, the environmental toll from coal is immense. In addition, fly ash
from coal is toxic and its disposal is subject to controversy. Natural gas, which is being promoted as a domestic solution to our demand for foreign oil, is also not without controversy. Regardless of the size of potential supplies and natural gas’ cleanliness as a fuel, it is still a limited hydrocarbon not quickly regenerated and emits CO2 when combusted. Hydraulic fracturing, also known as fracking, is becoming a popular method, especially in the nearby Marcellus Shale gas

Figure 1: Domestic Energy Consumption By Fuel Type (EIA)

Figure 2: Projected Oil and Natural Gas Production (Laherrere)
fields. Unfortunately, fracking is extremely controversial because it involves pumping potentially hazardous chemicals into the ground to fracture porous rock. Once broken, gas can seep through the rock to the borehole and be pumped to the surface. Problems arise when the chemicals do not return to the surface and instead find their way into the water table, which could potentially be aquifers used for potable water. Other cases have been reported where natural gas has seeped into ground water and videos have shown people lighting the water coming out their sinks on fire. Though natural gas is much cleaner and can be extracted domestically, it is clear there are obstacles to overcome before this fuel source is ready to supply a more significant portion of our energy needs. In the meantime, it will be relegated to a backup source used to meet peak demand when the baseload is not adequate.

Simultaneously, mankind’s thirst for energy is increasing quickly as populations and living standards around the world continue to rise. It is difficult to predict, but energy efficiency and conservation efforts will most likely not be enough to make up the difference in demand
placed on electric grids. Countries like China and India will continue to rely on cheap coal and oil to build their economies and infrastructures and to increase the standard of living of their people. Though India and China already employ nuclear power, the time and capital required to build new plants is immense and construction can not proceed as quickly as demand is increasing.

As a result of this increasing thirst for energy, an environmentally friendly alternative must be found if we are to continue to live in some kind of harmony with nature. There are several alternative sources of energy that can generate electricity with very few or no negative side effects to the planet. These sources, unlike fossil and nuclear fuels, are nearly limitless. Some of these sources are even consistent enough to be used for baseload generation. These sources include hydroelectric, whether it from dams, the currents in a river, or the waves in the ocean, power from water is consistent and offers the ability to provide, if not constant, at least predictable and controllable energy. Unfortunately, not all of the world is located near ideal hydraulic sources of electric, especially as one moves further inward from the oceans. Another renewable source, though not as easily accessible as hydro sources, is geothermal. Geothermal is very consistent and is capable of providing great amounts of energy. On the downside, geothermal is often very difficult to access and many of the best sources of geothermal power are incredibly deep, and thus expensive to reach. Geothermal is also not a practical source of energy over much of the world given its geographic and geological constraints and the expense required to reach it.

Wind power on the other hand is much more available the world over. Though the wind is not always predictable, it is a much more feasible over a much greater area of the planet. In addition, the technology required to harness the wind has been around for centuries if not
millennia. Wind energy is very scalable as well, with wind turbines ranging in size from several megawatts to as small as a few hundred watts. In addition, the Great Plains and coastal regions of the United States are home to relatively consistent winds that would lend themselves well to wind energy use; the Midwest is also rich in open land used primarily for farming where wind turbines would not hinder growth or serve as an aesthetic eyesore. Unfortunately though, wind farms require incredibly large amounts of land and suffer from low capacity rates, meaning a hundred megawatt farm may require several hundred square miles of land but may only generate 40-50MW of electricity at any given time or may generate 100MW for a day and then nothing the next. In addition, though wind patterns are well known and can be predicted, they can still not be controlled, and even nominally windy regions can have days where the wind is simply not blowing. Figure 4 below shows the optimal location of wind energy sites and their location relative to high voltage transmission lines.

If we are to break our dependence on fossil fuels without the help of nuclear power, we must seek out a steady and uncontroversial source that can be easily controlled and harnessed and done so in a predictable fashion. The only source capable of doing this is the same source that created this planet, the stars, and in particular, our nearby star, the sun. Solar energy can be harnessed in two ways, photovoltaic and concentrated solar thermal. Concentrated solar thermal may in fact be the oldest form of energy harnessed by man when it is alleged Archimedes of Syracuse used large mirrors to ignite the ships of the invading Roman fleet. Whether this is true or not may never be known, but it shows that it has been known since ancient times the potential power of the sun. In more modern times, solar energy is harnessed primarily by semiconducting materials in the form of photovoltaic (PV) cells. These cells can be put in series and parallel as desired and though PV cells can be put into large, megawatt size arrays, they are finding more
success as decentralized power sources on homes. Germany is leading the world in PV capacity because of state mandated utility regulations that subsidize panel costs and force utilities to buyback power at rates high above market value (Baetz). These mandates lead to a peak capacity of 12.1 GW that was reached in March of 2011 (Mims). Unfortunately, peak power from solar doesn’t coincide with peak grid demand, and the excess energy pushed onto the grid could reach dangerous levels (Newscientist). As a result, the subsidies will begin to be reduced in hopes of curbing these potentially dangerous spikes. Community energy storage systems could help alleviate these spikes but they could be years away, and would need to be managed by smart grid technology. Currently, the only solution to this issue is to quickly shut off small plants to prevent spiking. Needless to say, this is less than ideal, and would not be practical in an energy environment dominated by nuclear sources.

A much more ideal solution exists in the form of concentrated solar power. These plants exist on much larger scales, typically hundreds of megawatts, and utilize a much more efficient
Rankine or Brayton Cycle as opposed to the photoelectric and semiconductor efficiencies seen in PV panels. Solar thermal plants also offer another advantage over PV, the ability to store energy as heat and thus manage output. This ability, a result of thermal inertia, also allows heat to be stored for use long after the sun has gone down. This allows the plants to be used not just at the mercy of nature, but as controllable sources that are effective during peak grid usage. In addition to thermal capacitance, the turbines of some plants can be driven using natural gas as well. The United States also has access to a great wealth of solar rich lands that would be ideally suited for such plants, as seen in Figure 5. In fact, several such plants are under construction here in the US.

![SAI Across America](image)

Figure 5: Solar Thermal Potential in US (Department of Energy)

There are many different types of concentrating solar thermal plants here in the US, but almost all operate on a similar principle, which can be seen in Figure 6. These types of plants use
parabolic or rectangular Fresnal lens reflectors to focus sunlight onto heat conducting pipes pumping thermal fluid around the site. This thermal fluid can then be used to boil water or some sort of organic working fluid or refrigerant to drive a turbine. This turbine turns a generator and creates electricity. As is visible in Figure 6, various steam generator, super heater, and reheater combinations are available to maximize efficiency. Figure 7 shows the difference in a Fresnal lens and how it is derived from a conventional parabolic reflector.

Figure 6: Basic Solar Thermal Plant Operation (Quaschning)

Figure 8 shows another solar thermal setup, the heliostat. In this arrangement, a large field of mirrors focuses sunlight onto a small point on a tower. This heat can then run a boiler and operate on a similar Rankine cycle, or can force draft air to move through a tower, turning a turbine more like a controlled wind turbine.
These projects are great when capital and land are abundant, but that is not often the case, and even here in the US, these plants, though gaining in popularity are not prevalent and are less deployed than PV. One draw for PV is its scalability. Whether or not it is subsidized, photovoltaic power can be reduced in size to a couple of inches, and the ability to scale the system to meet various needs makes solar the more flexible choice. Currently, solar thermal on a small or residential scale is used only to heat water. Could a small scale system, small enough to fit nicely on a roof or in a backyard, be powerful or efficient enough to compete in price and scalability?

![Figure 7: Fresnal Lens from a Conventional Lens (Arenberg)](image)

Figure 7: Fresnal Lens from a Conventional Lens (Arenberg)
1.2 Project Overview

That is what this project hopes to find out. Previous work has been done to specify a solar collection system, and other work has modeled various fluids for use in the electricity generating loop. Further work has been done on low pressure expanders that can be used in place of turbines from the traditional Rankine Cycle in thermodynamics. This thesis hopes to accomplish two purposes.

1. Develop a physical experiment to test for feasibility of the concept and then to collect data for the purpose of validating a computer model.

2. Develop aforementioned model to simulate wide range of scenarios and find the appropriate size and configuration of a system to generate usable electric.

Both of these issues are addressed in the following report, as well as the results of data collection and simulated results from the Simulink model. The development of the a two loop
Rankine cycle system will be discussed in Chapter 2, while the development of the Simulink model will be discussed in Chapter 3.
Chapter 2: Experimental Setup

2.1 Introduction

This section serves as an overview of the physical system that will be used for data collection. The system is similar in setup to that used by Michael Nesteroff in the previous year to complete his thesis regarding solar energy collection. Upgrades to the I&C system in the form of a more permanent circuit board and changes to the LabView .VI will be made to compensate for the use of more sensors. In addition, the system consists of a primary and secondary loop, both of which will contain water for the scope of this experiment. In the future, it is hoped that an organic fluid or refrigerant can be used in hopes of generating actual steam and possibly creating electricity. However, because the setup currently exists now primarily to validate the models developed later in this report, and because of the challenges associated with working with volatile fluids such as refrigerants, water will be used as a stand in. Based off previous work, it is not expected that temperatures great enough to lead to phase change will be seen, however, basic heat transfer properties and power output properties can be found using water and changed appropriately in the model depending on the selected working fluids.

2.2 Experimental Layout and Mechanical Hardware

Figure 9 shows the experimental setup and where approximately the temperature sensors are positioned around the setup. There are two sensors not shown, one being the tank temperature, which is positioned approximately 3-5 inches into the tank. A second probe serves as an ambient air thermometer and is placed near the experiment. If one were to divide Figure 9 into half, the right half would serve as the primary loop, collecting solar energy and returning it to the storage tank. The left half would serve as the power loop, though in this case it will serve
only to dump heat and simulate a turbine and condenser. In reality, the primary loop feeds into and is fed directly into and from the tank, and does not have a heat exchanging loop.

Figure 9: Experimental Setup with RTDs (Nesteroff)

Figure 10 shows in better detail the true hardware associated with the primary loop. Seen in the picture is the tubing, the 100VAC pump -- which provided all pumping power on the primary loop, the bypass filter, the three-way valve allowing for flow control, and the Omega flowmeter. Also shown is the old breadboard circuit and battery, which as mentioned before has been replace with more permanent equipment. As water leaves the tank on the primary side, it travels to the pump via a three-way “tee.” From the pump, water is then fed to the three-way valve, where the position controls the flow to the solar collectors and redirects the remaining flow through a filter and back into the pump. The filter was added after testing began because some of the galvanized fittings had begun corroding. Figure 11 shows the solar collectors, two Silicon Solar SunMaxx-10s, both of which will be used. Individual manifolds were built with the
purpose of testing maximum tube efficiency and testing various concentrator configurations. These devices gather thermal energy and focus the energy into small copper nipples. The manifolds each hold of these tubes and water is heated as it is passed through the manifold. On the discharge side of each manifold is an RTD (resistance temperature detection) probe. After passing through both manifolds, which in the case of Figure 11 are backed by aluminum foil, the water is returned to the tank. Before entering into the tank, it passes through one last pipe nipple, where a final temperature is taken before it is added to the tank. It is important to note that the aluminum backing on the solar tube structures was not done by the manufacturer and was done by Mr. Nesteroff as part of his experiment. For this project, there will be no backing.

Figure 10: Primary Loop Hardware and Electronics
Figure 11: Solar Collection Tubes

Figure 12: Secondary Loop Test Setup
Figure 12 shows some of the secondary hardware used. Missing from the photo is a second flowmeter, which is identical to the flowmeter on the primary side. As it was not being used when these pictures were taken, it was left in the box to prevent damage. It will be placed between the pump and the radiator. Shown in Figure 12 is a standard automotive radiator placed in a metal housing to more easily mount two small DC fans. Also shown is the Laing D5 Solar pump; a small variable voltage DC pump that will be driven by a 12V battery. The flow will be controlled directly by the pump by way of pulse width modulation (PWM), done by an Arduino Duemilanove (Figure 13). The Arduino is a small open-source microcontroller running on a simplified version of the C programming language. Further discussion of the Arduino and software will take place in the next section.

![Arduino Duemilanove](image)

**Figure 13: DC Motor Controller, an Arduino Duemilanove (Arduino)**

### 2.3 Electronics, Instrumentation, and Control

As should be apparent by now, there is a somewhat sophisticated I&C system and electronic controls involved in data capture. Originally, a prototype board was made using a standard bread board and components until a final design was reached. This design was then put
onto a semi-permanent perforated bread board and soldered together. The design of the board can be seen in Figure 14. This board, using in conjunction with the Arduino board and a National Instruments 6211 Data Acquisition Device account for all the controls and data acquisition that will be done in testing.

![Image of Instrumentation and Control Board Schematic](image)

**Figure 14: Instrumentation and Control Board Schematic**

The board shown in Figure 14 will be wired to a 12VDC battery which powers the whole system, in parallel with a battery charger. Because power smoothing provided by the battery charger, it should not be necessary to add in additional filtering via a capacitor. All resistors shown in Figure 14 are 2 kohm. As seen on the left side of the figure, power for most of the instrumentation will be regulated down to 5 volts, this is done using an LM7905, which provided incredibly clean in initial testing. An LM7909 will be regulating to 10V on the other bus, and though it does not provide as clean a source of power as the 7905, the instrumentation on this
side is much less sensitive and mostly uses frequency modulation for data anyway. The 10V power will also be supplied to the Arduino board as the board sits near the test which may be a good distance from AC or USB power. The positive terminal of the battery will also be connected directly to the DC motor.

On the 5V side, seven of the eight thermal elements shown are 5kohm RTDs, with the remaining unmarked slot being reserved for an LM34 surface temperature probe. The final slot in the DB-9 (RS-232) connection is reserved for the solar pyranometer, which measures solar irradiation in $W*m^{-2}$. All nine of these connections will be fed to analog inputs on the NI-6211. On the 10V side, the two flowmeters will be fed into digital counter ports on the NI-6211, which will convert their square waves into flow rate information. Also coming in on that cable will be an analog out signal, which will be fed into an analog in port of the Arduino. This will serve as the DC motor control on the secondary loop by way of a low power MOSFET, in this case an IRF510. An analog signal between 0-5V will be fed to the Arduino, which will then output a modulated pulse wave with a duty cycle ranging between 0-100% in 20% increments. This logic level signal will drive the gate of the MOSFET, which will serve as the ground connection for the DC pump, with the battery ground the source and the motor negative the drain.

All of these signals are processed by a single VI in LabView, which provides real time monitoring on the front end and in the appropriate units. This data is also written to a tab delimited .txt file for further processing in MATLAB. The LabView VI also allows for control of the DC motor by manually changing the 0-5V analog signal to the Arduino, whose function was described above.
2.4 Testing Procedure

Two primary tests will be run, with several variations made to validate numbers across a broader range and to build more accurate look-up tables for possible use in the model. The initial test will involve validating the primary loop and confirming that the physical properties are accurate and the governing equations are working within reason. Since some work in this area was done by Mr. Nesteroff in the previous year, this testing will proceed quickly so that more robust testing can be done on the secondary side. Flow rates can be adjusted on each side to allow higher temperatures or more consistent heat flow away. In addition, DC fans on the radiator should allow for a more heat to be carried away by the radiator, allowing for a wider range of turbine conditions to be modeled in the future. Adjusting temperatures on each side allows for the model to be tested over a wider range of operating conditions and ensures that will translate more smoothly to an organic Rankine cycle. Discussion of the temperature range variations will take place in the Results section.
Chapter 3: Theoretical Setup

In parallel to the experimental setup and data collection, the second, and perhaps more important primary mission of this thesis is the development of a dynamic model capable of modeling in real time, the thermodynamics of the system. This model will serve as a basis for controls modeling and will allow various configurations to be simulated before being actually tested—an important ability given the unpredictable weather in the spring and fall season. It will also allow for parametric modeling to aid in configuration decisions as well as for providing data over ranges and for fluids not easily tested on the current configuration of the experiment. The model is broken into two distinct parts, the primary and secondary loop. Currently, the only connection between the two now is generic $q_{out}$ that will be added to the secondary side and subtracted from the primary side. The following chapter will give a detailed description of the two loops. The model is done in Simulink but can be controlled via MATLAB through the use of .m script files.

3.1 Thermodynamics

Before discussing the Simulink setup of the model, it is important to have an understating of the thermodynamics of the actual system. The experimental setup shown in the previous chapter will now be modeled using basic thermodynamics laws and principles. Figure 15 shows the primary and secondary loops, with the relevant variables shown. The model, like the system, begins with the primary loop, shown as the red loop. The primary loop is centered around the tank, where $T_{\text{tank}}$ is modeled as a time dependent capacitance to account for the thermal inertia of such a large mass of water. The energy balance for the tank, shown as Equation 1 in the model discussion includes $T_1$ and $T_4$, the temperatures in and out of the tank, respectively. This temperature difference is the basis of the model, as discussed in detail in the next section. This temperature
difference is ultimately based on two factors, \( \dot{m}_p \), the mass flow rate of the primary loop and \( G \), the solar radiation, or power, coming into the system. These relations will be discussed in depth below, but ultimately, the temperature difference and the temperature of the tank goes up as \( G \) goes up or flow rate decreases. Two other factors relevant to the tank temperature are the power out to the secondary loop, \( \dot{Q}_p \), and the power lost to convective and conductive losses, \( \dot{Q}_{\text{loss}} \).

On the secondary side, shown in Figure 15 the blue box behaves in a similar way. This time, starting at the tank, which will be referred to as the boiler for the secondary loop, energy is input into the boiler to boil a working fluid. The overall behavior of the secondary side is shown in Figure 16, a thermodynamic T-s diagram. In the boiler, the working fluid, in this case -- most likely a refrigerant -- undergoes a phase change; that is it goes from position 2, a sub-cooled liquid, to position 3, a superheated vapor. In the process, it reaches a saturation temperature where it changes from a liquid to a gas but exists as a mixed phase at a constant temperature until it reaches pure vapor, at which point its temperature again begins increasing. Whether the substance is superheated or saturated steam, it then exits the boiler and heads to the turbine, or in the case of this model, a vapor separator, which separates out liquid if the fluid is two phase. As vapor passes through the turbine, it gives up its energy in the form of pressure and quality which is converted to physical work that turns the turbine. This work drives a generator and generates electricity and is represented as the transition from point 3 to point 4 on Figure 16. After the turbine, the fluid must finish condensing, which involves converting the remaining vapor to liquid. This can be done by dumping the waste heat or using it in a co-generation setup,
Figure 15: Thermodynamic Setup (Nesteroff)

Figure 16: Thermodynamic Diagram of Secondary Loop (Wither)
which it is hoped in this case, could be used to heat water for the home. This transition from saturated or superheated vapor to saturated or sub-cooled liquid is shown in Figure 16 as the change from 4 to 1. In a basic system as shown, the fluid is then re-pressurized and returned to the boiler, which is shown in Figure 16 as the transition from 1-2. For this system though, since vapor and liquid are separated, the intermediate step of reuniting the flows occurs in an open feed water heater.

The proceeding discussions will center on how the model handles these thermodynamic behaviors. Because of the dynamic and time dependent nature of the model, differences are used on variables with capacitance. In a simple thermodynamic calculation, total values would be used, but again, because of the dynamic nature of the model, the differences in energy in and energy out are used in lieu of the total values when calculating states and values. The proceeding discussion will discuss this in greater detail.

3.2 Primary Loop

The primary loop, for the purpose of the model, consists of the storage tank, the two manifolds, energy out to the secondary side and a loss element. It is centered around the equation:

\[ mcT' = mcT_4 - mcT_1 - \dot{Q}_p - \dot{Q}_{\text{loss}} \]  

(1)

where \( m \) is the mass of the tank, \( c \) is the specific heat of water, \( T \) is temperature, \( Q_p \) is power to the secondary side, and \( Q_{\text{loss}} \) are losses from the tank and hose to outside the system. Position 1 is immediately following the exit of the tank, and in the case of Equation 1 represents energy being carried out of the tank by the flow. Position 4 is the exit from the manifolds and the entrance back to the tank with the newly energized flow. For reference Position 2 will follow from the
pump (not included in model) and Position 3 will be between the two manifolds. Figure 17 shows the primary loop model.

Beginning at the summation block, the energy balance between the manifolds is added to the loss from the system losses and the secondary loop, depicted as a step function. This number is enthalpy, in this case specific enthalpy given in Joules/kg. This number is then divided by the product of the specific heat and mass of the tank, and is integrated in accordance with Equation 1. This number is the temperature of the tank, and is used to determine energy loss and addition for the next step. From the top, there is the loss of energy from the water being carried away from the tank, which is handled by having the tank temperature subtracted from the manifold exit temperature, which is then treated as a single variable, in this case $\Delta T$.

Figure 17: Primary Loop Simulink Model
Then inner workings of the manifold can be seen in Figure 17. Here the two addition blocks in the top row serve as the manifolds. They are supplied energy from the constant block in the bottom right corner, which in this case serves as the solar irradiation on the area divided by \( \dot{m}c \) to keep the addition consistent with temperature. Before being added to the system flow, the input energy is multiplied by an efficiency factor. Originally, the efficiency was to be an experimentally defined constant, however, a literature review revealed an efficiency equation, shown as Equation 2 (Energiesystem) and shown in Simulink as Figure 19. \( T_m \) is the mean of the input and exit temperature of the manifolds, Since the temperature gain at steady state across the manifolds is relatively small, the model was simplified to give the two manifolds the same efficiency. More precise results can be obtained by using separate efficiencies per manifold, and different experimental setups may necessitate that. Table 1 gives the value of the coefficients. \( T_a \) is the ambient temperature, and \( G \) is the solar irradiation striking the manifold.

Figure 18: Manifold Subsystem
\[ T_{out} = T_{in} + 2 \left( \frac{G_{in} A \eta}{m_p c_f} \right) \]  
\[ \eta = \eta_0 - a_{1a} \frac{T_m - T_a}{G} - a_{2a} \frac{(T_m - T_a)^2}{G} \]  

Figure 19: Efficiency Subsystem

<table>
<thead>
<tr>
<th>Coefficient Values for Efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \eta_0 )</td>
</tr>
<tr>
<td>( a_{1a} )</td>
</tr>
<tr>
<td>( a_{2a} )</td>
</tr>
</tbody>
</table>

Table 1: Efficiency Coefficients

Returning to the main system depicted in Figure 17, system loss is represented in the lower right hand corner and is governed by Equation 4. \( \dot{Q}_{loss} \) is the sum of conductive and

\[ \dot{Q}_{loss} = \sum \frac{k}{L} A \left( T - T_{amb} \right) + \sum h A \left( T - T_{amb} \right) \]  

(4)
convective losses, which are numerous in the experimental setup. Therefore, for simplifying the model, a single loss coefficient is used in place of $\Sigma \frac{k}{L} A + \Sigma h A$. This is done because there is no data for finding $k$ values in much of the hardware. Finally, a step function was added to stand in as a load from the secondary side. This value can be varied as necessary to simulate whatever condition is desired for a thermal load.

### 3.3 Secondary Loop

The secondary loop, for the purpose of the model consists of the inner loop of the tank, which will be referred to as the boiler or vaporizer, a steam separator, a turbine and condenser—which act as a thermal load and are the only source of loss on the secondary side, and an open feedwater heater, where the separated flows are mixed together and return to the boiler. Because of the nature of SIMULINK, the method of modeling is not as intuitive as setting up a basic thermodynamics problem. The model is closed off completely but unlike a regular Rankine cycle, one cannot just send a flow through the loops. In addition, there is phase change occurring in this loop, which means that the fluid can exist in one of three conditions: subcooled, superheated, or a two phase, saturated mixture. As a result, the system must be able to monitor itself, determine which condition it is in, and apply the appropriate equations. The separation of the flows also requires they be put back together to assess how much power is removed from the system. This detail will be discussed in depth later.

To begin, the secondary loop is shown in Figure 20. Starting at the boiler, Energy is introduced into the system. This is shown in Figure 21, where a sinusoidal input is shown. A sinusoid was chosen as it most closely can mimic the temperature profile in the tank, which will directly affect the energy into the system. Since there is no coupling of the primary and

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secondary loops, this was the best stand in for a typical profile the boiler may see. Once the energy in, which is in watts, is converted to a specific enthalpy, it is sent to a summing block, where the energy out of the system, also in specific enthalpy, is subtracted from the energy in to determine the net energy into or out of the system. This interaction is expressed in Equation 5

\[ \Delta h_{out} = \frac{1}{\dot{m}} (Q_{in} - Q_{out}) \]  

(6)
where $Q_{out}$ is actually the sum of the work out from the turbine and the heat out from the condenser. $\Delta h$ is used instead of $h$ because the next blocks, shown in Figure 22 and Figure 23 use an integrator block. These subsystems are part of the larger subsystem called “boiler conditions out,” which can be seen in Figure 20 and in more detail in Figure 24. They are governed by Equations 7 and 8 and are dependent on the current state of the fluid, whether it be subcooled, saturated, or superheated, to determine which coefficients apply to the gain. This is done by a case selector, which uses Boolean logic on temperature, quality, and the heat in to determine the case. From the $\Delta h$ the subsystem outputs a temperature, in degrees Celsius, and a quality. Figure 25 shows a generic T-h diagram for one of the modeled fluids. It includes the vapor dome and shows the increase in $h$ dependent of temperature and how it is affected in the mixed phase region.

\[ \dot{T} = \frac{\Delta h}{c} \quad \text{for } T \neq T_{\text{sat}} \]  

\[ \text{Figure 22: Boiler Exit Temperature} \]
\[
\dot{x} = \frac{\Delta h}{h_{fg}} \quad \text{for } T = T_{\text{sat}}
\]  

Figure 23: Boiler Exit Quality

Figure 24: Boiler Exit Conditions Subsystem
The next block, the steam separator, shown in Figure 26, takes the temperature and quality from the boiler exit and converts it into specific enthalpies of steam and liquid that are then sent to the turbine/condenser. As for this is accomplished, an if block determines the condition of the fluid, and the appropriate action block is then called. For a subcooled fluid ($x<0$) Equation 9 gives the function for converting temperature to enthalpy. This same equation holds true for superheated fluids. The difference is the value of $c$, which is different for the two, as well as $h_0$ which is different. For the subcooled substance, it is the enthalpy at 0 degrees C, but for superheated, it is the saturation enthalpy of gas. For a fluid at saturation, the phases have known enthalpies for the liquid and gas phase, and that block just outputs those constant values.

$$h = cT + h_0$$ (9)
The steam separator also calculates the total energy of the flow before it is separated to be used later in determining return conditions. This is done using Equation 10.

\[ h = x h_g + (1 - x) h_f \]  

(10)

Figure 26: Steam Separator Subsystem

From the steam separator, the flow is, with a fraction, \( x \), of the flow going to the turbine condenser and the remainder, \( 1-x \), going to the open feed water heater. The turbine and condenser share a block, as shown in Figure 27. For the model, it is assumed that the turbine exit conditions are \( x=0.9 \) at 3 bar pressure. This allows a specific enthalpy to be picked and makes the turbine power out dependent only on enthalpy in and quality as shown in Equation 11. For the condenser, it is assumed that some specific heat, \( q \), is taken out of the condenser, making the condenser dependent only on quality for its power out as shown in Equation 12. These two assumptions can be easily changed to test a variety of circumstances or can be made more accurate or dynamic depending on needs and available data. Power out from the turbine and
condenser are then added together to get a total power out of the system. This power is sent to the open feed water heater and to the boiler. This is the power out of the system that is used to determine the net input into the system.

\[
\dot{W} = \dot{m}(h_{in} - h(P = 3\,\text{bar}, x = .9)) \quad (11)
\]

\[
\dot{Q} = \dot{m}(\Delta h_{\text{cond}}) \quad (12)
\]

Figure 27: Turbine Condenser Subsystem

Finally, the Boiler Return Conditions subsystem, Figure 28, gives the temperature and quality of the return flow to the boiler. It does this by first finding the enthalpy of the returning flow by subtracting the power out from the enthalpy of the flow initially leaving the boiler, as shown in Equation 13. It then processes compares the enthalpy to the saturation enthalpies of liquid and gas, determines the state, and calls the appropriate action block, which use Equations 9 and 10 in reverse to find the temperature and exit quality.
\[ h_{\text{return}} = h_{\text{boiler,exit}} - \sum_i \frac{\dot{Q}_{\text{out},i}}{x_i m_i} + \sum_i \frac{\dot{W}_i}{x_i m} \] (13)

Figure 28: Boiler Return Conditions Subsystem
Chapter 4: Results and Discussion

For this section, the two portions of this project will be merged. Actual data will be used to validate the primary loop and to make projections for the secondary loop model. To recap what data was collected, Table 2 shows what variables were monitored, in what positions, and how.

Table 2: Data Collection

<table>
<thead>
<tr>
<th>Variable</th>
<th>Details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature</td>
<td>8 Thermistors: 1 on the exit of each manifold (2), one on each of entrances or exits of the tank (4), 1 for the water in the center of the tank, and one for ambient temperature</td>
</tr>
<tr>
<td>Flow Rate</td>
<td>Two flow meters, one for each loop</td>
</tr>
<tr>
<td>Solar Insolation</td>
<td>Pyranometer normal to the solar collection tubes</td>
</tr>
</tbody>
</table>

For this discussion, only the tank temperature, solar insolation, and flow rate on the primary loop. Poor weather conditions prevented data from being collected this spring and thus no data exists for the secondary loop. As mentioned above, the purpose of data from the experiment will be to validate the Simulink model.

4.1 Primary Loop Results and Validation

Though several days of data was collected for the primary loop, most of it involved the testing of various solar concentrators. These devices negate the efficiency calculation provided by Fronhauffer and no effort was made to quantize their efficiency. As such, only data from testing day 1, November 8th, will be used. Data collection began shortly after sunset and continued through most of the day, ending just after sunset. Solar insolation for the day is shown below in Figure 29. As stated before, this is the actual solar insolation coming in normal to the plane of the tubes. This data was then plugged directly into the primary loop model and the loss
coefficient was adjusted appropriately until an almost exact match was found, as shown in Figure 30.

Figure 29: Solar Insolation on November 8, 2010

Figure 30: Experimental versus Model Tank Temperature
The data shown in Figure 30 is also dependent on flow rate, the mass of water in the tank, the specific heat of the water, and the ambient temperature. Constants were used for three of these variables, shown in Table 3. For ambient temperature, this data was recorded, but the signal quality was poor and several errors made the data nearly unusable. As a result, the Simulink signal generator was used to closely mimic, though in a more stepped fashion, the ambient temperature. Finally, the experimentally adjustable loss coefficient was manually tweaked over several iterations until the results produced those shown in Figure 30. The final value of the loss coefficient was .0165. It is believed that the initial source of error was a result of the capacitance of the water and manifolds that were left out overnight in the cold November air. Though the tank internal temperature was initially around 33°C, the water remaining in the system and the manifolds themselves no doubt cooled down over night, when the testing began, which was right after sunrise, the low insolation at the time was not quickly overcome this capacitance. After this test, a final test of the model was run. Though no data exists to give an idea of energy loss as a result of a thermal load on the secondary side, for modeling purposes, a step function is added to the tank energy balance. In the case shown in Figure 31, a dummy 500 watt load was applied to the tank at around the 4.2 hours mark. This load was meant to simulate a load from the secondary loop. Though a load from the secondary loop is likely to be dependent on the tank temperature and thus more sinusoidal or parabolic in shape, the lack of hard data

<table>
<thead>
<tr>
<th>Table 3: Primary Loop Constants</th>
</tr>
</thead>
<tbody>
<tr>
<td>m_dot</td>
</tr>
<tr>
<td>C</td>
</tr>
<tr>
<td>m_tank</td>
</tr>
</tbody>
</table>
makes this prediction difficult to do accurately, thus a moderate load was applied just to give an order of magnitude idea of the temperature loss that may be seen in the tank.

![Graph showing temperature change over time](image)

**Figure 31: Primary Loop Simulation with 500 Watt Load at 4.2 Hours**

### 4.2 Secondary Side Modeling

As was mentioned previously, no data was able to be collected to validate the secondary side, therefore all data for the secondary side is based on predictions and guesses based on experience and realistic expectations. Before continuing with this discussion, a recap of previous research on the topic of fluid selection is relevant for this section.
Jake Wither performed a parametric analysis of several refrigerants with low boiling points that may be ideally suited for this project. His analysis ultimately led to the selection of R600a as the refrigerant of choice for the secondary side model, though he suggested 3 other fluids too based on his research, these fluids are shown with some of their properties in Figure 32.

![Table: Refrigerant Properties (Wither)](image)

Again, this chart shows that R600a’s boiling points are most in line with temperatures reasonable for this system. Though not shown, a pressure of 10 bar was used for modeling. The boiling point of R600a at 10 bar is 66.84 C. though that temperature was never reached under normal operation conditions, Mike Nesteroff was able to achieve that temperature using simple reflectors, a more complex reflector may offer an even higher temperature differential for boiling.

For the actual model simulation, several other variables were selected; more so than on the primary loop. These constants are shown in Table 4. Figure 25 shows the full T-h diagram.
for n-Pentane, a similar fluid, at 3 and 10 bar. Also important is the input power into the boiler, which is shown below in Figure 33. This curve is generated from the sin wave function.

Table 4: Secondary Side Constants

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>m_dot</td>
<td>.06kg/s</td>
</tr>
<tr>
<td>c_vapor</td>
<td>2.232 kJ/kg/C</td>
</tr>
<tr>
<td>c_liquid</td>
<td>2.634 kJ/kg/C</td>
</tr>
<tr>
<td>h_fg</td>
<td>267.7 kJ/kg</td>
</tr>
<tr>
<td>h_f</td>
<td>497.7kJ/kg</td>
</tr>
<tr>
<td>h_g</td>
<td>765.4 kJ/kg</td>
</tr>
<tr>
<td>h(T=0C, p=10bar)</td>
<td>327.1 kJ/kg</td>
</tr>
<tr>
<td>h(p=3bar, x=.9)</td>
<td>670.6 kJ/kg</td>
</tr>
</tbody>
</table>

Figure 33: Power into Boiler
in Simulink and is meant represent the approximate temperature curve of the water tank/boiler. Only a few outputs will be looked at to get an idea of what is going on in the system. Several assumptions were made, some rather broad, to complete the model since no data was available for a thermal load turbine, extreme liberty was taken with assuming conditions from the turbine and condenser. At the boiler exit, the conditions are shown in Figure 34. One can see from the

![Figure 34: Boiler Exit](image)

figures that the quality and temperature go through three distinct phases, sub-cooled, saturated, and superheated. It is apparent as a small upward line, and flat line at \( T = T_{\text{sat}} \) and a superheated section that is somewhat sinusoidal. As for quality, a quick upward jump to .4, followed by a slower rise to 1 where it stays for the remainder of time. From these outputs, and using the assumptions made about the turbine, a power out from the turbine can be found, and is shown relative to boiler power in Figure 35. It is not possible to make assumptions about turbine efficiency or overall system efficiency based off the assumptions made for the model, but Jake Wither’s parametric analysis does provide some insight into the efficiency of a system given a temperature in and out, a pressure in, and the pressure ratio of turbine. This data is shown for
reference sake in Figure 36. This efficiency is based off the returning saturated liquid back to the boiler.

Figure 35: Turbine Power Out v Boiler Power in

Figure 36: R600a System Efficiency Plot for Varying Expander Inlet Temperatures and Pressure Ratios, with Inlet Pressure of 10 Bar (Wither)
Chapter 5: Conclusion and Recommendations

5.1 Experimental Summary

This report has laid out the experimental setup of a system for collecting data on the thermal portion of a residential scale solar thermal electrical plant. From a system viability perspective, the system has shown that it is capable of achieving, if not sustaining, the required temperatures needed to boil a low pressure refrigerant. With this system viability confirmed, more testing still remains for the secondary loop to gather data for sufficient modeling. In addition, work on the low pressure expander continues, and part of this work should include determining expander efficiency. This efficiency can be used to improve the efficiency of the parametric models of the fluids and the dynamic modeling of the secondary loop. In fact, it will be crucial to developing a realistic loop. The radiator in position in the secondary loop of the test setup is coupled to two DC motors which can be controlled using a PWM duty cycle, just like the motor, therefore, a wide range of thermal loading opportunities exist for testing. The aperture surface area can also be increased to bring in more solar energy, and produce higher temperatures with high flow rates. Overall, the model is very scalable and should serve well into the future in a variety of tests to determine the overall feasibility of this project.

5.2 Modeling Summary

As was seen, the primary loop of the system has been validated using real data with water as a working fluid. The option exists to replace water with an oil that may boil at a much higher temperature, assuming these temperatures can be achieved. It would also be advised to include temperature capacitance of the manifolds and the water left in them over night. A cold winter night would drop temperature in the system before a pseudo steady state is reached. The opposite
effect may happen on a balmy summer night, with temperature spiking quickly before returning
to a steady climb.

5.3 Recommendations

Data collection remains to be completed on the secondary loop, as an unseasonably cold
and rainy spring made data collection impossible. It is believed that a few days of collection
should allow a relationship between tank temperature and secondary loop return temperature to
equate to a total power out of the tank and into the secondary loop. This would essentially allow
the two loops to be coupled into a single model. Finally, as was mentioned above, work can be
done to improve the secondary loop. There are three key points to be improved upon.

1. Development of turbine efficiency and work equations to accurately model whatever
   form of expander is ultimately used.
2. Development of equations of more accurate assessment of the energy out of the
   condenser/radiator setup.
3. Addition of losses to the secondary loop, similar to that of the primary loop.

If these three points can be adequately addressed, complete simulation of the system under any
conceived conditions should be possible.
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